

"Fundamentals of Rydberg Atoms and  
Molecules »  
Workshop "YEA" (Young Excited Atomix )



# Properties and dynamics of a cold sample of Rydberg atoms

Pierre Pillet

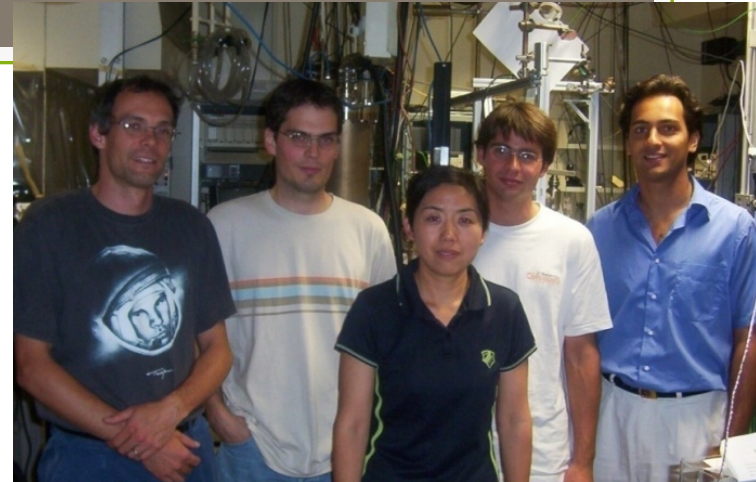
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COHERENCE School  
and YEA meeting

Pisa, 20 – 22 September 2012

# Cold Rydberg atoms / Ultracold plasmas

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Jianming Zhao  
Andrea Fioretti  
Patrick Cheinet  
Daniel Comparat  
Pierre Pillet



## Collaborations:

**On few-body effects with Phil F. Gould, Univ of Connecticut and Jianming Zhao, Univ of Shanxi**

**On dipole blockade with the group of Ennio Arimondo, Univ of Pisa**

**On ultracold plasmas with Thomas F. Gallagher, Univ of Virginia and Ducan Tate, Colby College**

**On collective excitation of a pair of atoms in the dipole blockade regime with Philippe Grangier, Antoine Browaeys et al., Institut d'Optique**



## La Grenouille qui se veut faire aussi grosse que le Boeuf

Une grenouille vit un boeuf

Qui lui sembla de belle taille.

Elle, qui n'était pas grosse en tout comme un oeuf,

Envieuse, s'étend, et s'enfle, et se travaille,

Pour égaler l'animal en grosseur,

Disant : « Regardez bien, ma soeur ;

Est-ce assez ? dites-moi ; n' y suis-je point encore ?

- Nenni. - M' y voici donc ? - Point du tout. - M' y voilà ?

- Vous n'en approchez point. » La chétive pécore

S'enfla si bien qu'elle creva.

Le monde est plein de gens qui ne sont pas plus sages :

Tout bourgeois veut bâtir comme les grands seigneurs,

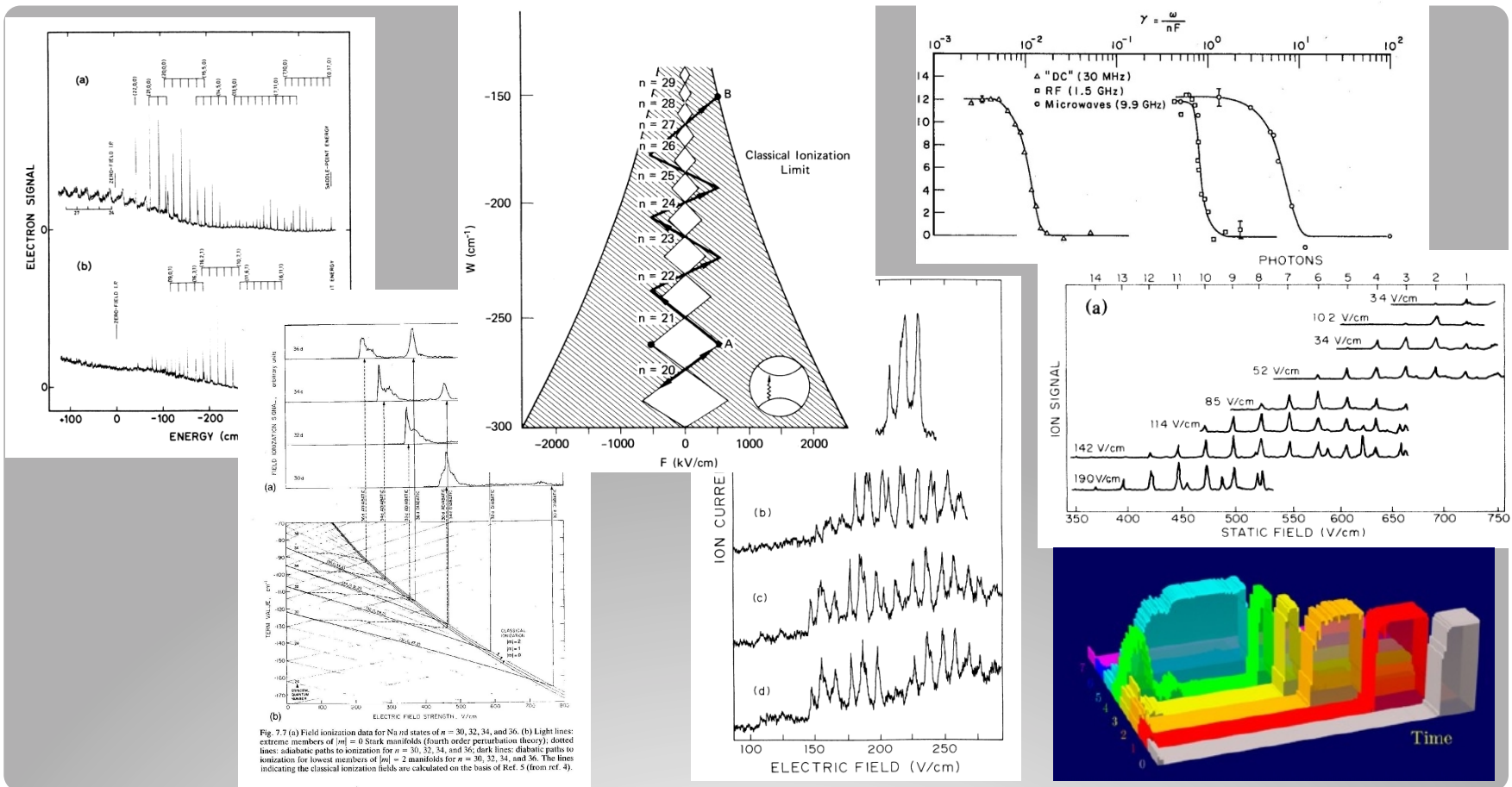
Tout petit prince a des ambassadeurs,

Tout marquis veut avoir des pages.



# Jean de Lafontaine (1621 – 1695)

n = 200 000 ! Very sensitive to any perturbation



# Rydberg atoms versus electric field

**Behaviors of Rydberg atoms in electric field? From static field to quantum field**  
 Stark spectroscopy, photoionization of H, electric field ionization, microwave ionization, multiphoton transitions, microwave assisted collisions, Rydberg atoms in cavity

# WHY **C**old Rydberg atoms? **C**ollective effects

The atoms are cold and Rydberg

**C**ooperativity, **c**oherence, **c**orrelation

Due to

**I**nteraction, **i**nterference, **i**ntrication (entanglement)

# Main properties of a cold Rydberg gas

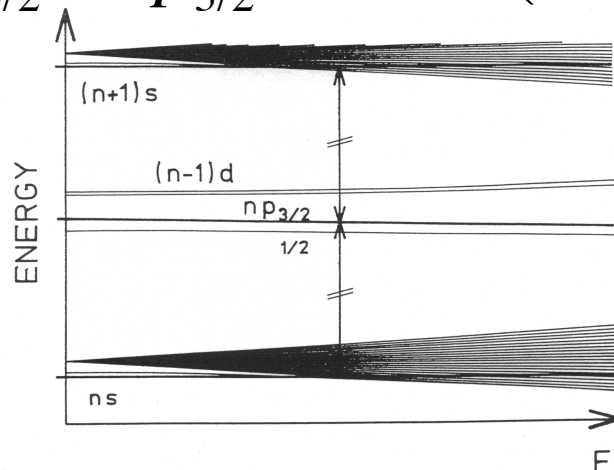
- Cold: frozen gas
- Rydberg: Strongly interacting
- Long-range forces: Penning ionization
  
- Consequence: at the frontier of solid state physics and plasmas physics

# Dipole – dipole interaction

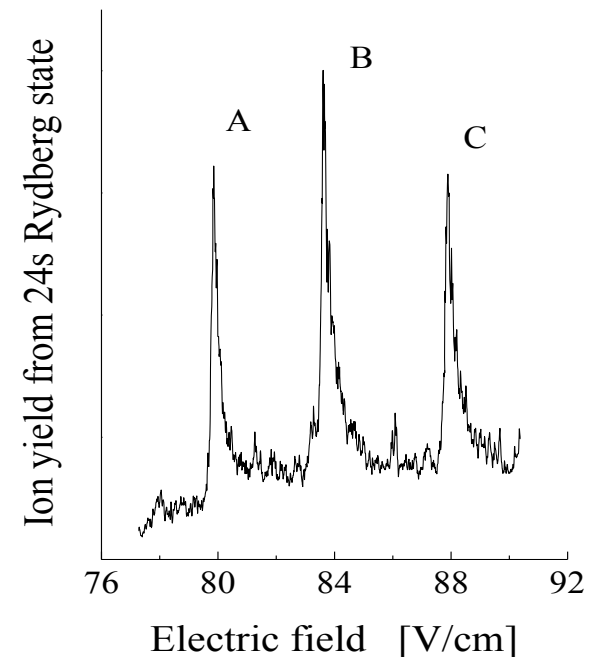
Förster resonances

# Förster dipole-dipole resonances (exchange of internal energy)

- Experimentally introduced by T.F. Gallagher (P.R.L. 40, 1362 (1981), in Rydberg-Rydberg collisions
- Case of Cs  $np_{3/2}$  ( $n < 42$ )  
 $np_{3/2} + np_{3/2} \rightarrow ns + (n+1)s$



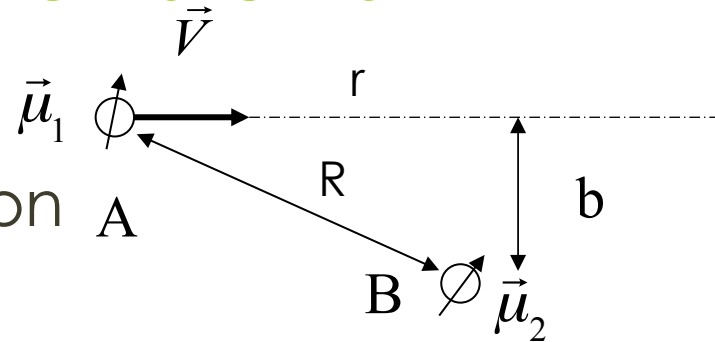
$m_1 + m_2$   
 A  $1/2 + 1/2$   
 B  $1/2 + 3/2$   
 C  $3/2 + 3/2$





# Dipole-dipole collisions

- Atomic beam
- Dipole-dipole interaction



$$W = \frac{\vec{\mu}_A \cdot \vec{\mu}_B}{R^3} - 3 \frac{(\vec{\mu}_A \cdot \vec{R})(\vec{\mu}_B \cdot \vec{R})}{R^5}$$

$$W = \frac{\mu_A \mu_B (1 - 3 \cos^2 \theta)}{R^3} = \frac{\mu_A \mu_B (-2r^2 + b^2)}{(r^2 + b^2)^{5/2}}$$

$$\mu_A = \langle ns | er | np \rangle \quad \text{and} \quad \mu_B = \langle (n+1)s | er | np \rangle$$

## Collision time and impact parameter

$$|\psi(t)\rangle = a_1(t)|pp\rangle + a_2(t)|ss\rangle$$

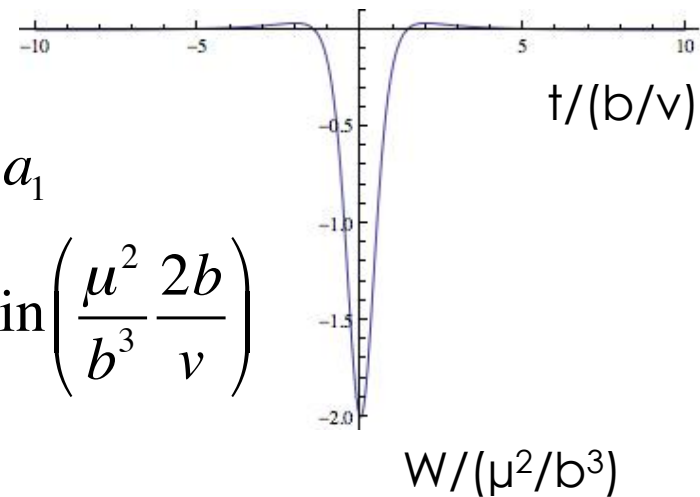
$$i\dot{a}_1 = W(t)a_2 \quad \text{and} \quad i\dot{a}_2 = \delta a_2 + W(t)a_1$$

$$\delta = 0: \quad a_2 = -i \sin\left(\int_{-\infty}^{\infty} W(t') dt'\right) = i \sin\left(\frac{\mu^2}{b^3} \frac{2b}{v}\right)$$

$$\sigma = \pi \int_0^{\infty} \sin\left(\frac{2\mu^2}{vb^2}\right) 2b db = \frac{\pi^2 \mu^2}{v}$$

$$b_0 \approx \sqrt{\frac{\mu_A \mu_B}{v}} \quad \text{and} \quad \tau_0 = \frac{2b_0}{v} \approx \frac{\sqrt{\mu_A \mu_B}}{v^{3/2}}$$

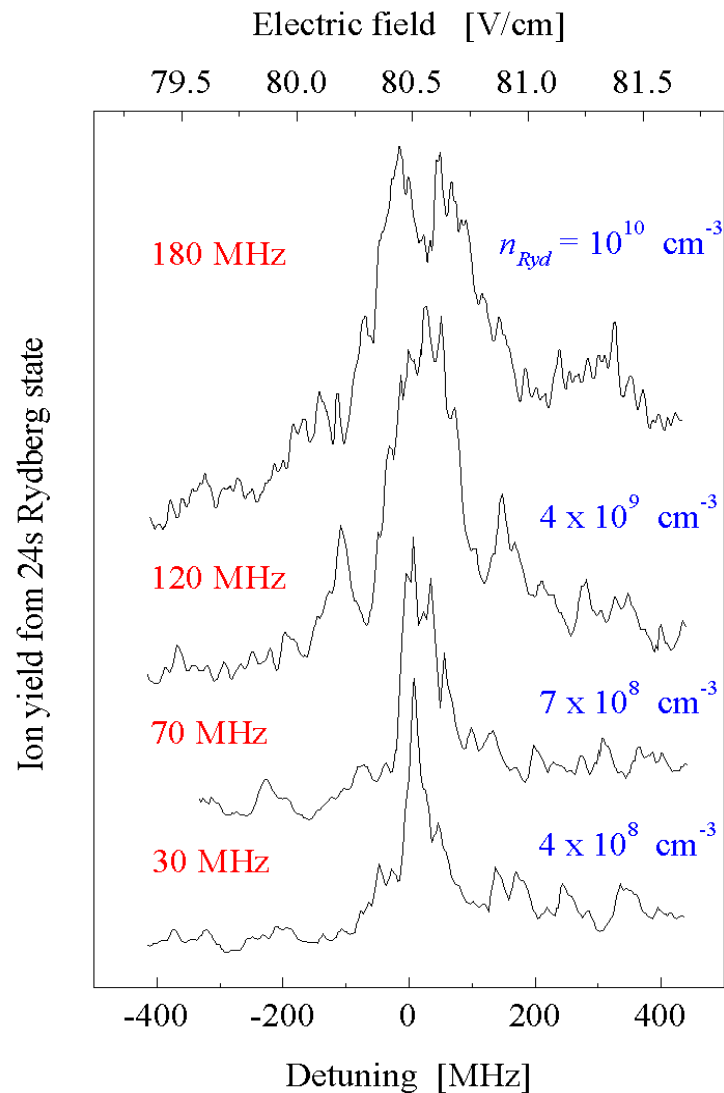
- Very large impact parameter  $\sim 1 \mu\text{m}$  for  $n=20$  and  $v=300 \text{ m/s}$
- Collision time  $\sim 10 \text{ ns}$



# Slow collisions and frozen Rydberg gas approximation

- The width of the resonance is the inverse of the collision time and becomes narrower for slow collisions
- For cold atoms  $v \sim 0.1$  m/s, the impact parameter is  $\sim 50$   $\mu\text{m}$  (comparable to the volume size) and the collision time  $\sim 1$  ms (larger than the Rydberg lifetime)
- No motion (at least when the experiment starts  $< 1$   $\mu\text{s}$ ) ; the atoms move their size 100nm
- The atoms interact altogether
- **FROZEN RYDBERG GAS approximation**
- What about collective effects: many-body effects?

# Dipole-dipole interactions in a frozen Rydberg gas



$$23p_{3/2}(|m_j| = 1/2) + 23p_{3/2}(|m_j| = 1/2)$$

$$\rightarrow 23s + 24s$$

Population Transfer  $\sim 10\text{-}15\%$

Interaction between the closest neighbors leads to a too small

width:  $W_{typ} \approx \frac{\mu_1 \mu_2}{R_{AB}^3} < 1.5 \text{ MHz}$

The frozen Rydberg gas cannot be explained in the framework of two-body effects

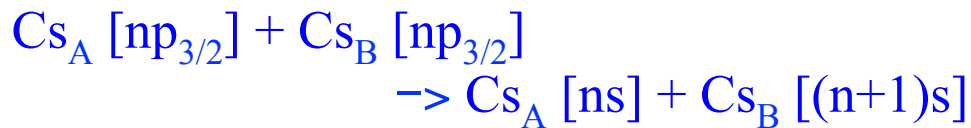
- Many-body effects in a frozen Rydberg, I. Mourachko, D. Comparat, F. de Tomasi, A. Fioretti, P. Nosbaum, V. Akulin et P. Pillet, Phys. Rev. Lett., 80, 253 (1998)
- Resonant dipole-dipole energy transfer in a nearly frozen Rydberg gas, W.R. Anderson, J.R. Veale, and T.F. Gallagher, Phys. Rev. Lett., 80, 249 (1998)

# Many-body effects

Interplay with a two-body effect and many-body phenomena

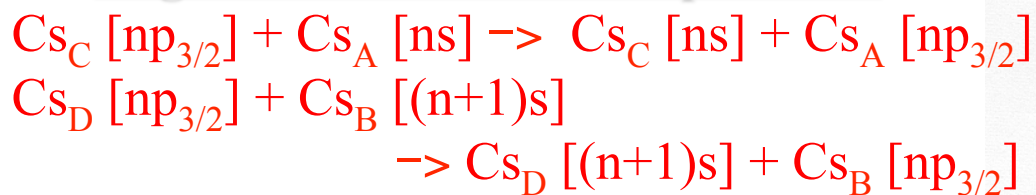
Elementary processes:

I - Resonant transfer of internal energy



(resonant for a given electric field)

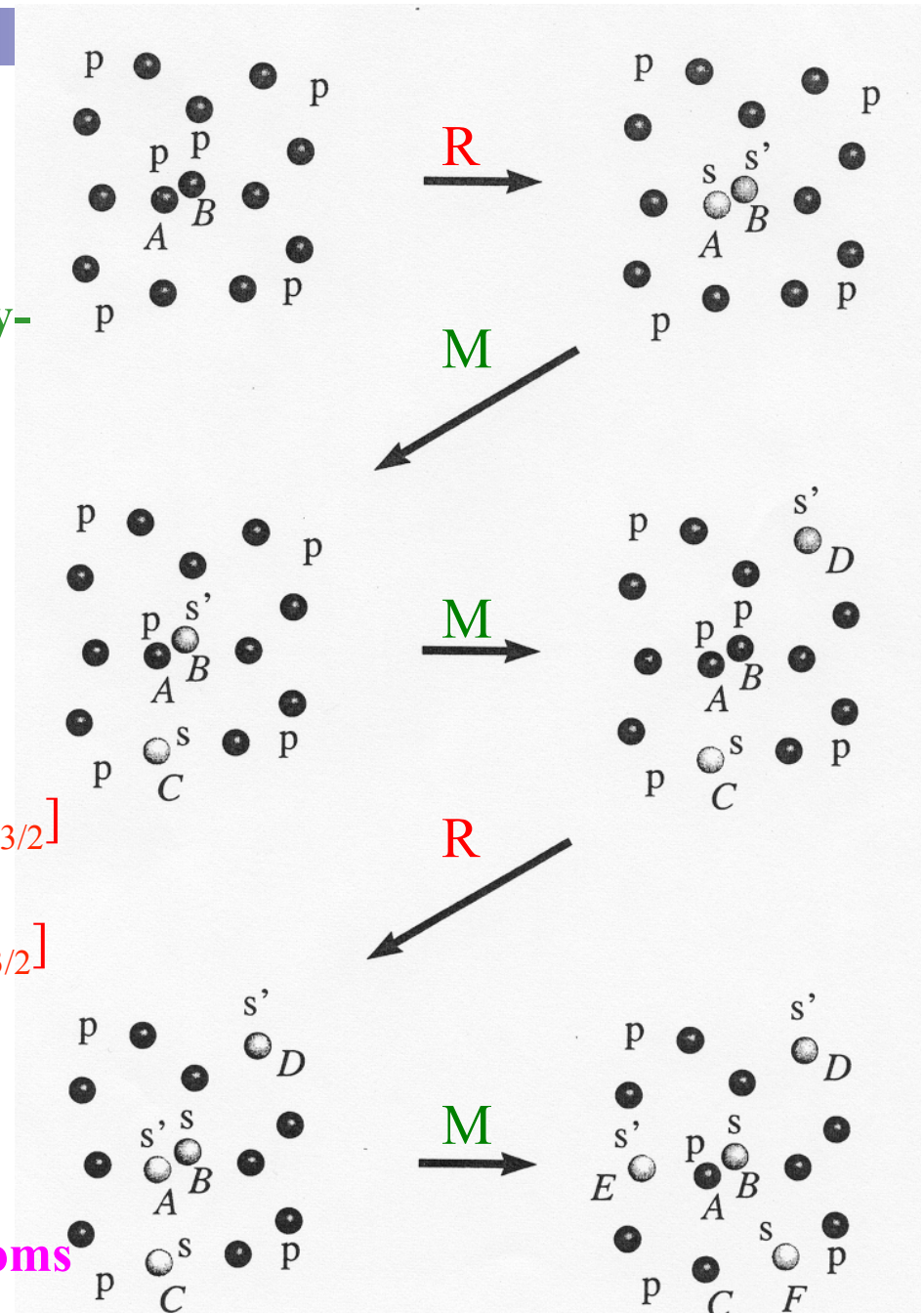
II - Migration of the reaction products



(no sensitive to the electric field)

Mourachko et al., PRA 70, 031401 (2004)

Importance of the “fluctuations”  
in the Rydberg density of pairs of close atoms



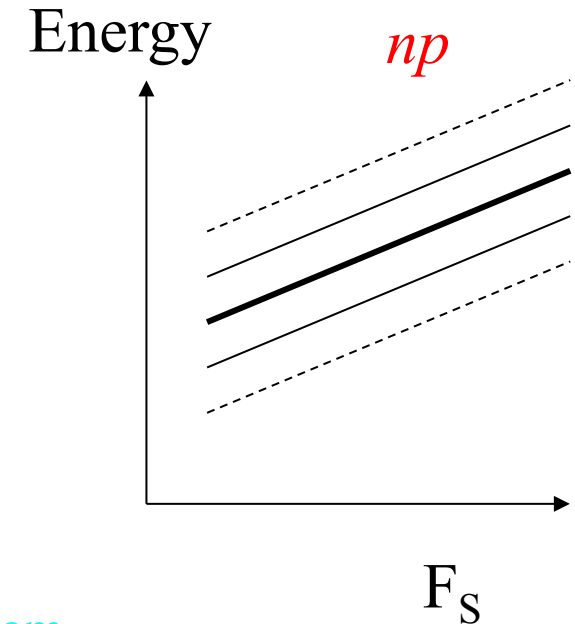
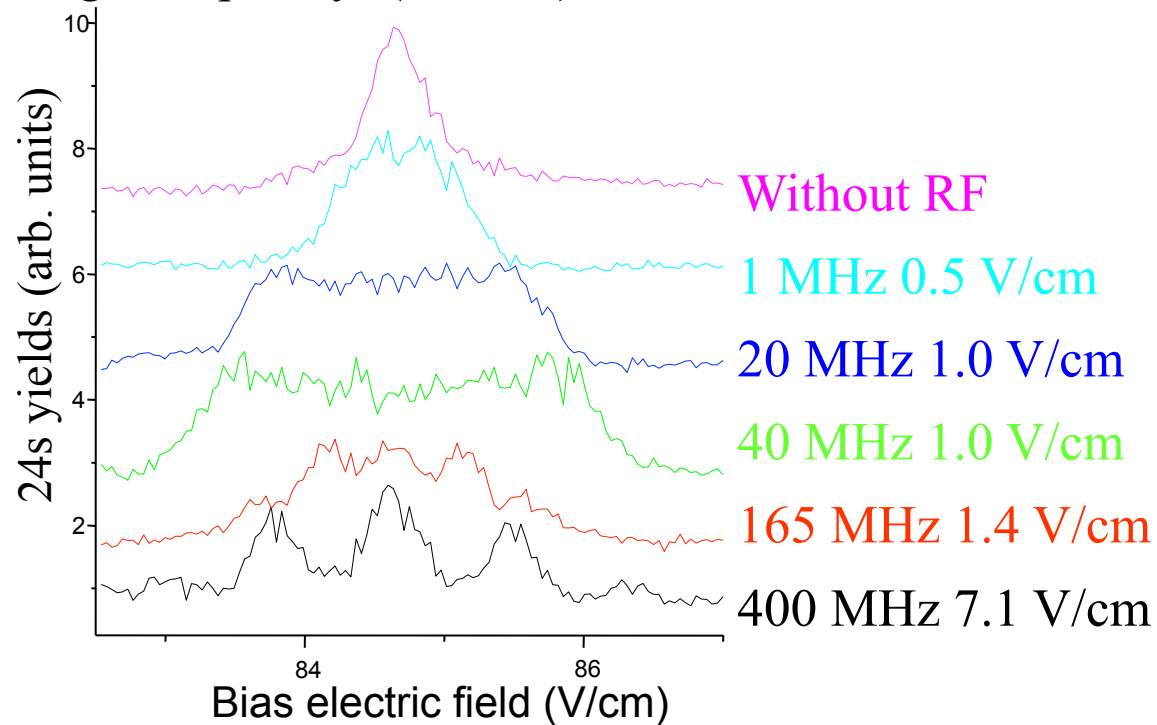
# Dipole – dipole interaction assisted by microwave

Förster resonances

# Frozen Ryddberg gas: Dipole-dipole interaction assisted by microwave frequency

$$F = F_S + F_{RF} \cos(\omega t)$$

- Low frequency ( $\omega \ll \Gamma$ ) broaden lineshape
- High frequency ( $\omega \gg \Gamma$ ) sidebands



Unpublished LAC data

# Many-body and few-body processes

Four-body resonance

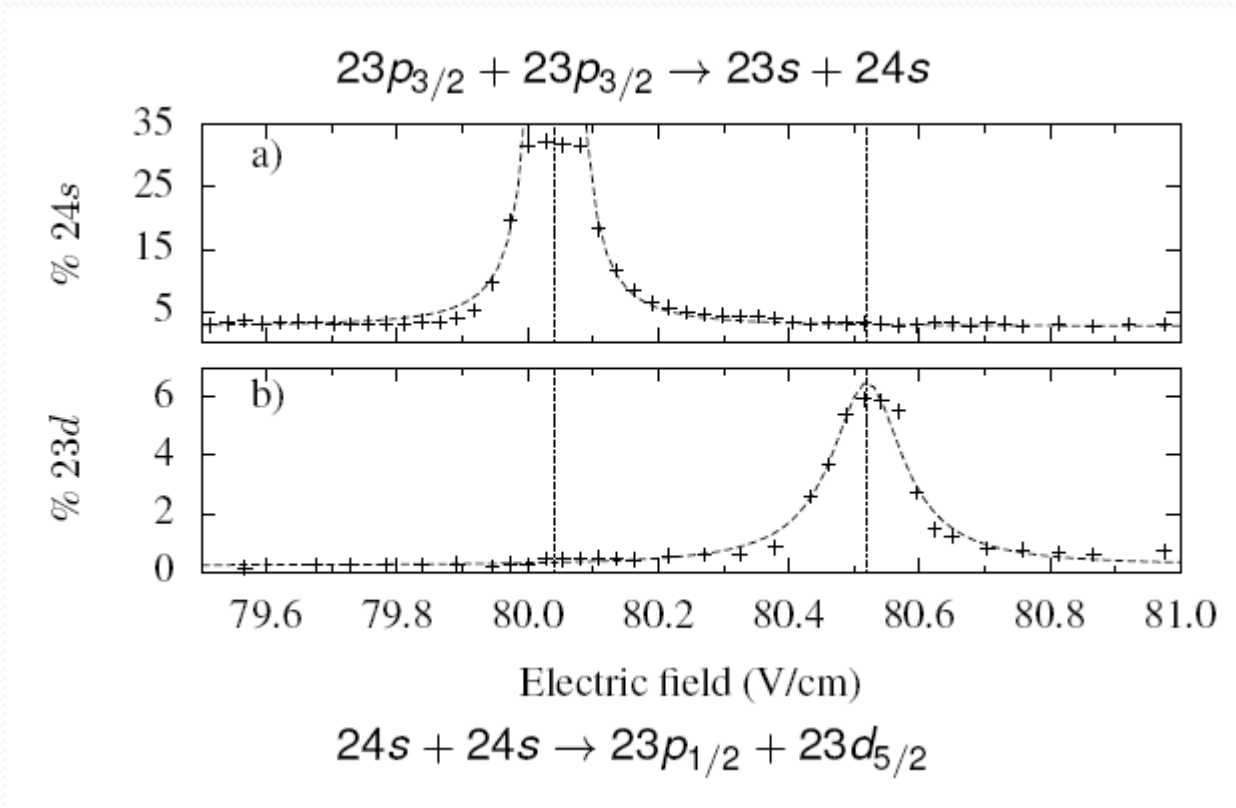
J. H. Gurian, P. Cheinet, P. Huillery, Y. Bruneau, A. Fioretti,  
J. Zhao\*, P. L. Gould\*\*, D. Comparat, P. Pillet

Phys.Rev.Lett. 108, 023005 (2012)

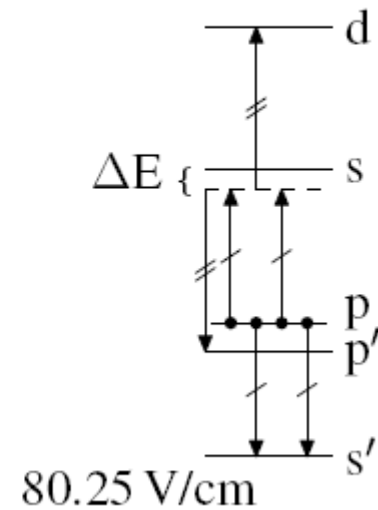
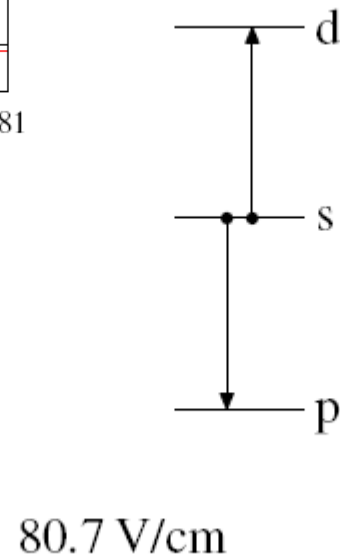
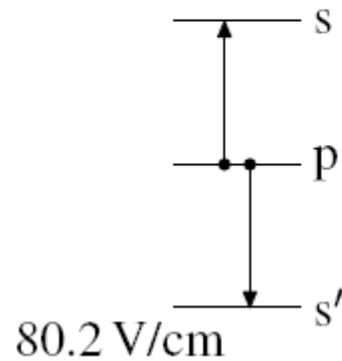
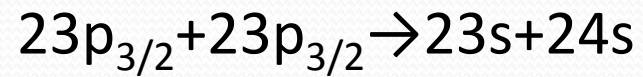
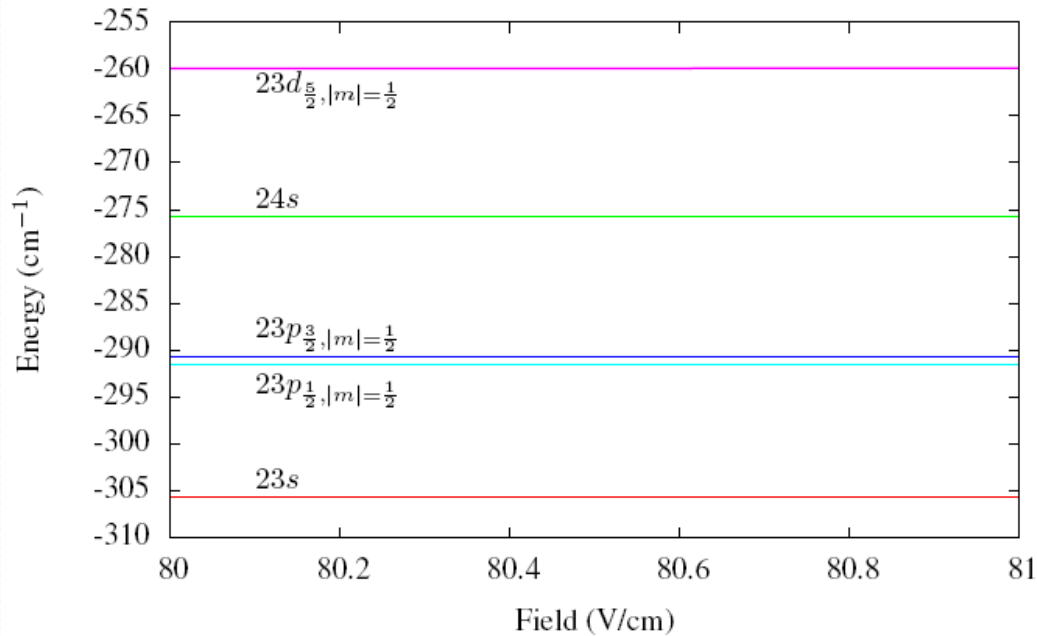
Collaborations with University of Shanxi\*, University of  
Connecticut\*\*



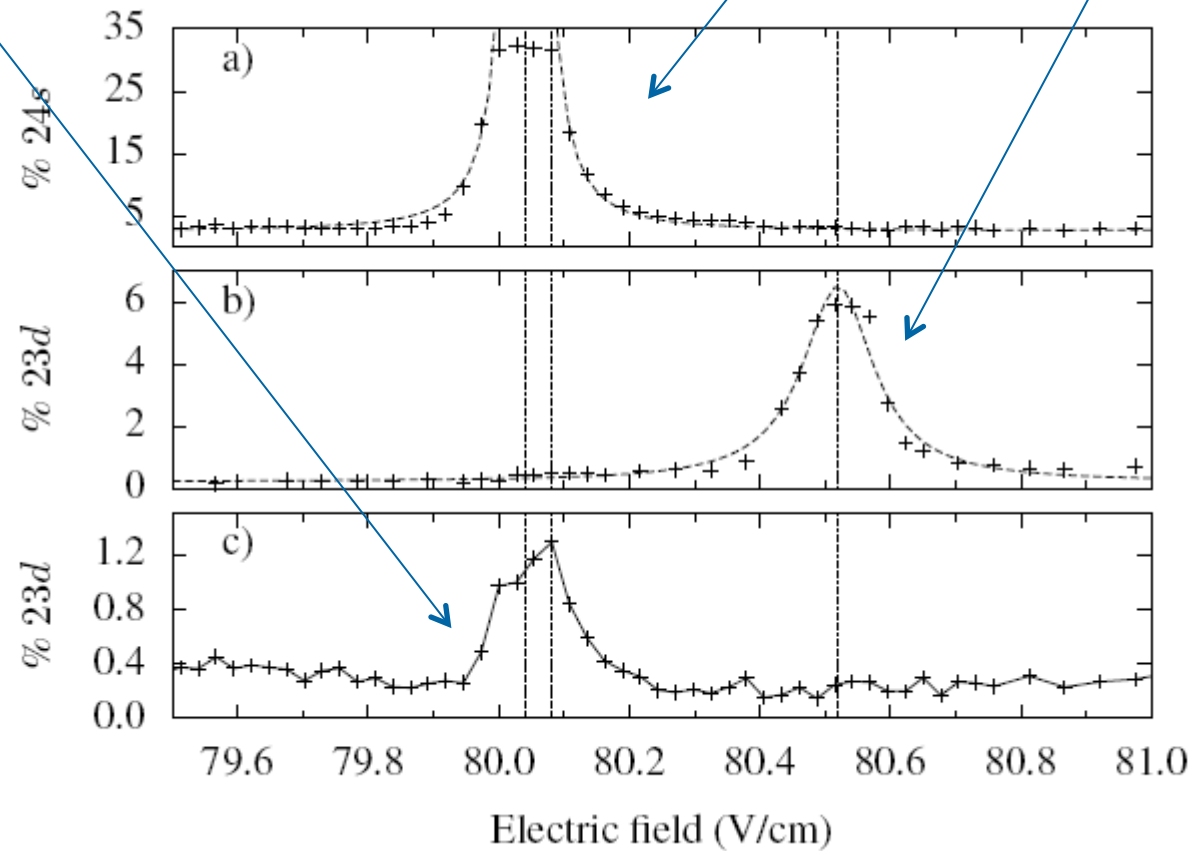
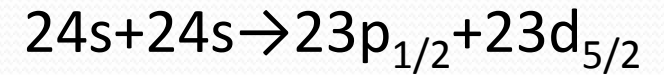
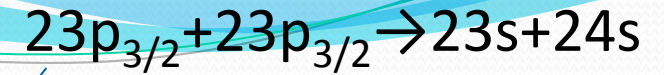
# Two examples of two-body Förster resonances



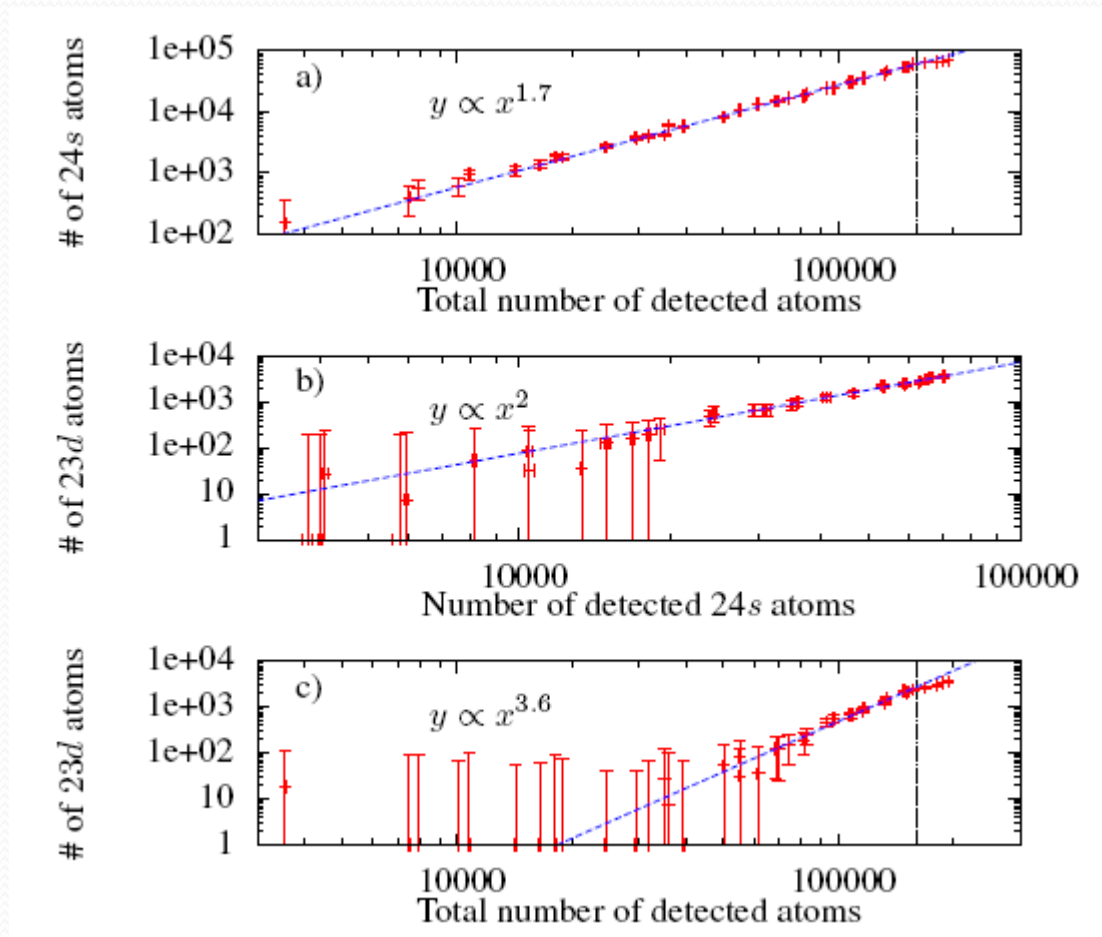
# 4-body Förster resonance



# Four-body resonance



# Intensity behavior as $\sim N^4$



# A-few-body interactions

- Difficult to characterize in a gas
- Difficult to discriminate 3, 4, 5... - body effects
- Observed when the two-body processes are saturated
- With cold Rydberg atoms we can have several signatures (transfer, resonance)
- Four-body resonance occurs here for low  $n$
- Many configurations may be more efficient can be studied, and four, six or eight-body Förster resonances could be demonstrated
- We create an entanglement of a few atoms